

Heavy Top Quark Production in the Bestest Little Higgs Model at the LHC



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Outline



- The Bestest Little Higgs Model
 - Motivation
 - Scalar Sector
 - Gauge Sector
 - Fermion Sector
- Heavy Top Quark Production
 - Pair Production
 - Single Production
- Results
- Conclusions

The Bestest Little Higgs Model

Schmaltz, Stolarski, Thaler (2010), hep-ph/1006.1356v1



- Difficult to generate Higgs quartic coupling that preserves custodial SU(2) symmetry in LH models
- Most LH models predict $\frac{m_T}{m_{W'}} \simeq \frac{m_t}{m_W} \simeq 2$
 - Precision EW physics constrain heavy gauge boson masses $m_{W'} \gtrsim 2-3 \text{ TeV}$
 - Avoiding fine-tuning in the top sector requires $m_T \lesssim 1-2 \text{ TeV}$
- Bestest LH Model generates a custodially symmetric Higgs quartic coupling with relatively light top partners

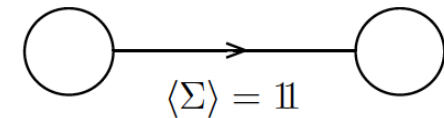
Collective Quartic Coupling



- $SO(6)_A \times SO(6)_B \rightarrow SO(6)$

$$\Sigma = e^{i\Pi/f} e^{2i\Pi_h/f} e^{i\Pi/f}$$

Global: $SO(6)_A$ $SO(6)_B$



Gauged: $SU(2) \times U(1)$

- 15 scalars:
 - 2 complex Higgs doublets (4 d.o.f. each) : h_1, h_2
 - $SU(2)_L$ triplet: ϕ
 - $SU(2)_R$ triplet: η
 - Real singlet: σ

$$\Pi_h = \frac{i}{\sqrt{2}} \begin{pmatrix} 0_4 & h_1 & h_2 \\ -h_1^T & 0 & 0 \\ -h_2^T & 0 & 0 \end{pmatrix}$$

$$\Pi = i \begin{pmatrix} \phi_a T_L^a + \eta_a T_R^a & 0 & 0 \\ 0 & 0 & \sigma/\sqrt{2} \\ 0 & -\sigma/\sqrt{2} & 0 \end{pmatrix}$$

$$V_{\text{quartic}} = \frac{\lambda_{65}}{2} \left(f \sigma - \frac{1}{\sqrt{2}} h_1^T h_2 + \dots \right)^2 + \frac{\lambda_{56}}{2} \left(f \sigma + \frac{1}{\sqrt{2}} h_1^T h_2 + \dots \right)^2$$

- Integrating out σ gives:

$$V_{\text{quartic}} = \frac{\lambda_{56} \lambda_{65}}{\lambda_{65} + \lambda_{56}} (h_1^T h_2)^2 = \frac{1}{2} \lambda_0 (h_1^T h_2)^2$$

Scalar Potential and EWSB



- Scalar Potential below $f \sim 1$ TeV:

$$V_{\text{higgs}} = \frac{1}{2}m_1^2 h_1^T h_1 + \frac{1}{2}m_2^2 h_2^T h_2 - B_\mu h_1^T h_2 + \frac{\lambda_0}{2}(h_1^T h_2)^2$$

- EWSB: $\tan \beta \equiv \frac{\langle h_{11} \rangle}{\langle h_{21} \rangle} = \frac{m_2}{m_1}$

$$v_{\text{EW}}^2 \equiv \langle h_{11} \rangle^2 + \langle h_{21} \rangle^2 = \frac{1}{\lambda_0} \left(\frac{m_1^2 + m_2^2}{m_1 m_2} \right) (B_\mu - m_1 m_2) \simeq (246 \text{ GeV})^2$$

- Higgs spectrum below f is a 2HDM

$$M_{h^0, H^0}^2 = \frac{B_\mu}{\sin 2\beta} \mp \sqrt{\frac{B_\mu^2}{\sin^2 2\beta} - 2\lambda_0 B_\mu v^2 \sin 2\beta + \lambda_0^2 v^4 \sin^2 2\beta}$$

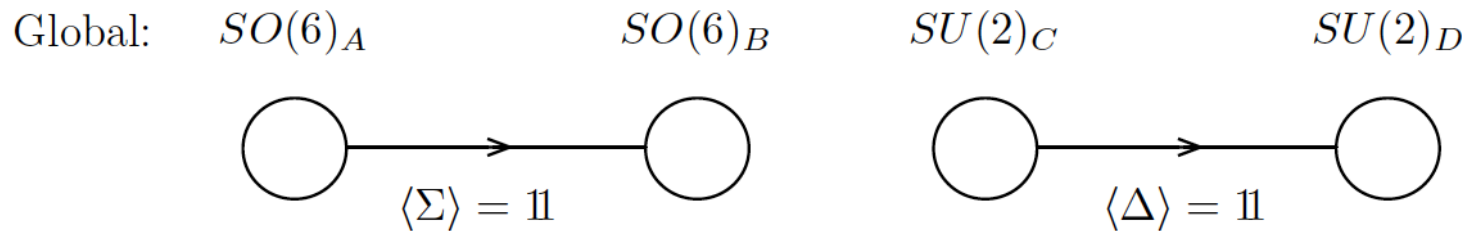
$$M_{A^0}^2 = M_{H^\pm}^2 = m_1^2 + m_2^2 = \frac{2B_\mu}{\sin 2\beta} - \lambda_0 v^2$$

$$M_{h^0}^2 < M_{A^0}^2 \approx M_{H^\pm}^2 < M_{H^0}^2$$

Gauge Sector



- Introduce another independent sigma model at a scale $F > f$



Gauged: $SU(2)_A$ $U(1)_Y$ $SU(2)_B$ $SU(2)_A$ $SU(2)_B$

$$\Sigma = e^{i\Pi/f} e^{2i\Pi_h/f} e^{i\Pi/f} \quad \Delta = e^{2i\Pi_d/F}, \quad \Pi_d = \chi_a \frac{\tau^a}{2}$$

- Σ breaks $SO(6)_A \times SO(6)_B$ to diagonal subgroup at scale f
- Δ breaks $SU(2)_C \times SU(2)_D$ to diagonal subgroup at scale F

$$\mathcal{L} = \frac{f^2}{8} \text{tr} (D_\mu \Sigma^\dagger D^\mu \Sigma) + \frac{F^2}{4} \text{tr} (D_\mu \Delta^\dagger D^\mu \Delta) \quad A_i^{(6)} = A_i^a T^a, \quad A_i^{(2)} = A_i^a \frac{\tau^a}{2}$$

$$D\Sigma = \partial\Sigma + ig_A A_1^{(6)} \Sigma - ig_B \Sigma A_2^{(6)}, \quad D\Delta = \partial\Delta + ig_A A_1^{(2)} \Delta - ig_B \Delta A_2^{(2)}$$

Gauge Boson Masses



- After EWSB, the gauge boson masses become:

$$M_\gamma^2 = 0$$

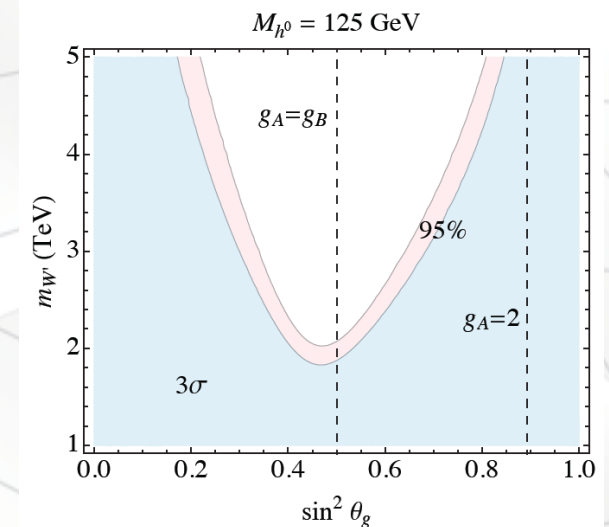
$$M_Z^2 = \frac{1}{4} (g^2 + g'^2) v^2 - (g^2 + g'^2) \left(2 + \frac{3f^2}{f^2 + F^2} (s_g^2 - c_g^2)^2 \right) \frac{v^4}{48f^2}$$

$$M_W^2 = \frac{1}{4} g^2 v^2 - g^2 \left(2 + \frac{3f^2}{f^2 + F^2} (s_g^2 - c_g^2)^2 \right) \frac{v^4}{48f^2}$$

$$M_{Z'}^2 = \frac{1}{4} (g_A^2 + g_B^2) (f^2 + F^2) - \frac{1}{4} g^2 v^2 + \left(2g^2 + \frac{3f^2}{f^2 + F^2} (g^2 + g'^2) (s_g^2 - c_g^2)^2 \right) \frac{v^4}{48f^2}$$

$$M_{W'}^2 = \frac{1}{4} (g_A^2 + g_B^2) (f^2 + F^2) - M_W^2$$

- $\rho = 1$ at $O(v^4/f^2)$
- Heavy Gauge Boson masses $\sim F > f$
- We choose $\tan\theta_g \equiv g_A/g_B = 1$



Fermion Sector



- To build Yukawa interactions, Fermions must transform under $SO(6)_A$ or $SO(6)_B$

$$SO(6)_A: \quad Q^T = \left(\frac{1}{\sqrt{2}}(-Q_{a1} - Q_{b2}) \quad \frac{i}{\sqrt{2}}(Q_{a1} - Q_{b2}) \quad \frac{1}{\sqrt{2}}(Q_{a2} - Q_{b1}) \quad \frac{i}{\sqrt{2}}(Q_{a2} + Q_{b1}) \quad Q_5 \quad Q_6 \right)$$

$$SO(6)_B: \quad (U^c)^T = \left(\frac{1}{\sqrt{2}}(-U_{b1}^c - U_{a2}^c) \quad \frac{i}{\sqrt{2}}(U_{b1}^c - U_{a2}^c) \quad \frac{1}{\sqrt{2}}(U_{b2}^c - U_{a1}^c) \quad \frac{i}{\sqrt{2}}(U_{b2}^c + U_{a1}^c) \quad U_5^c \quad U_6^c \right)$$

$$SU(2)_A \text{ doublet:} \quad Q_a'^T \rightarrow \frac{1}{\sqrt{2}}(-Q_{a1}', iQ_{a1}', Q_{a2}', iQ_{a2}', 0, 0)$$

$$SU(2)_B \text{ singlet:} \quad U_5^{cT} \rightarrow (0, 0, 0, 0, U_5'^c, 0) \quad S = \text{diag}(1, 1, 1, 1, -1, -1)$$

$$\mathcal{L}_t = y_1 f Q^T S \Sigma S U^c + y_2 f Q_a'^T \Sigma U^c + y_3 f Q^T \Sigma U_5'^c + \text{h.c.}$$

Breaks
 $SO(6)_A$ & $SO(6)_B$

Preserves
 $SO(6)_B$

Preserves
 $SO(6)_A$

- All 3 terms collectively break the symmetries protecting the Higgs
 \therefore Top Yukawa & radiative corrections to V_{higgs} can be generated

Heavy Top Quark Masses



- After EWSB, the fermion masses become (assuming $y_2 \neq y_3$):

$$M_t^2 = y_t^2 v_1^2 \quad \text{where} \quad y_t^2 = \frac{9y_1^2 y_2^2 y_3^2}{(y_1^2 + y_2^2)(y_1^2 + y_3^2)}$$

$$M_{T_{au}}^2 = (y_1^2 + y_2^2) f^2 + \frac{9v_1^2 y_1^2 y_2^2 y_3^2}{(y_1^2 + y_2^2)(y_2^2 - y_3^2)}$$

$$M_{T_{ad}}^2 = (y_1^2 + y_2^2) f^2$$

$$M_{T_5}^2 = (y_1^2 + y_3^2) f^2 - \frac{9v_1^2 y_1^2 y_2^2 y_3^2}{(y_1^2 + y_3^2)(y_2^2 - y_3^2)}$$

$$M_{T_6}^2 = M_{T_{b2}}^2 = M_{T_{b5}}^2 = y_1^2 f^2$$

Charge 2/3: T_{au}, T_{b2}, T_5, T_6

Charge -1/3: T_{ad}

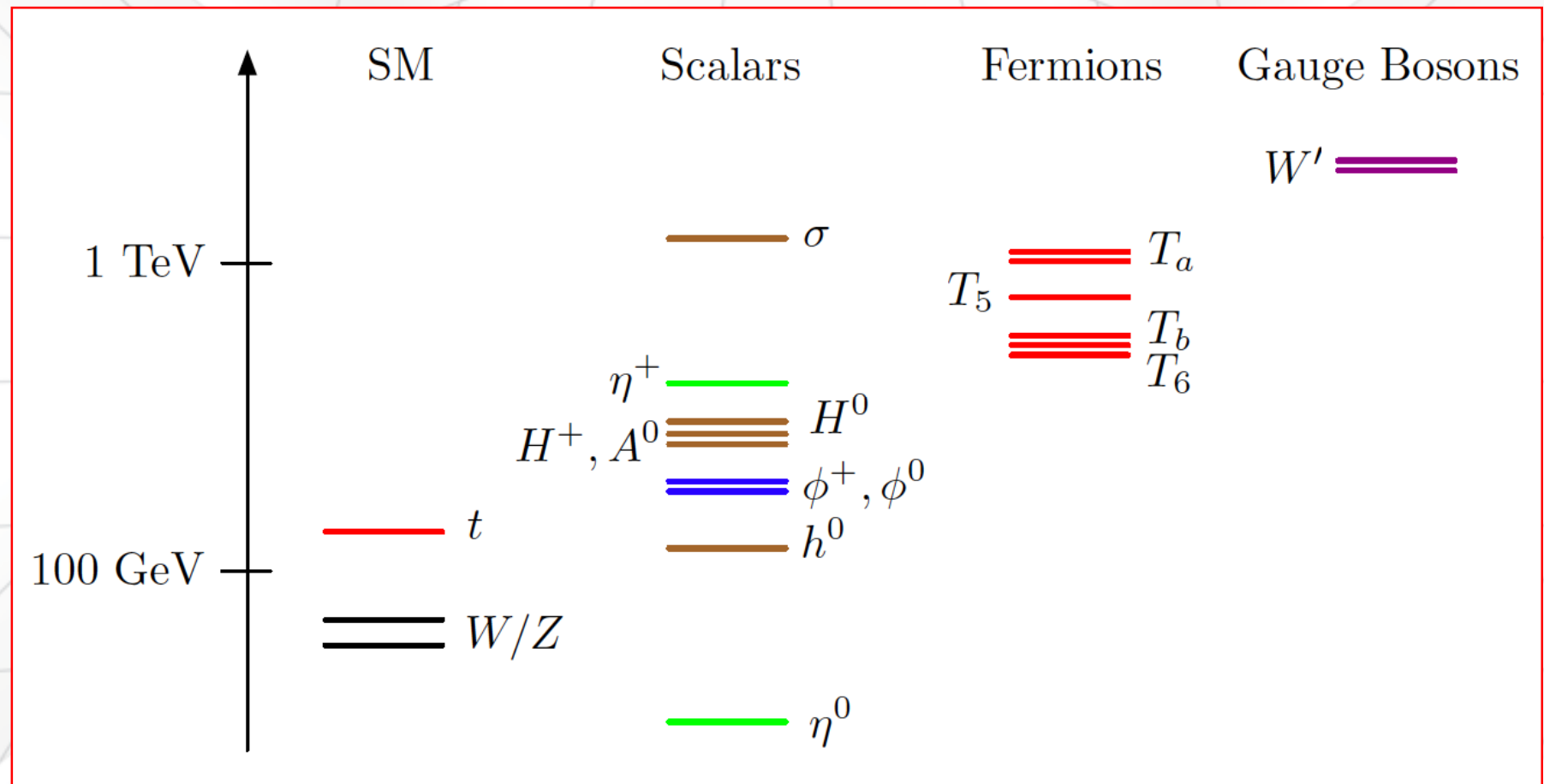
Charge 5/3: T_{b5}

- Heavy Top Masses $\sim f < F$, lighter than Heavy Gauge Bosons

$$M_{Z'}^2 = \frac{1}{4} (g_A^2 + g_B^2) (f^2 + F^2) - \frac{1}{4} g^2 v^2 + \left(2g^2 + \frac{3f^2}{f^2 + F^2} (g^2 + g'^2) (s_g^2 - c_g^2)^2 \right) \frac{v^4}{48f^2}$$

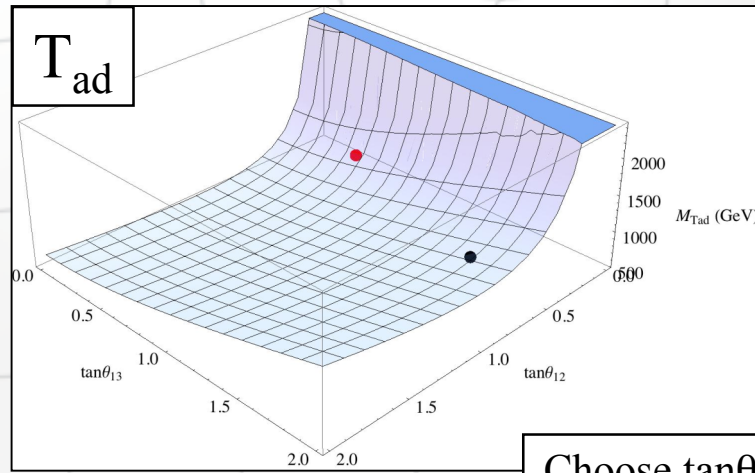
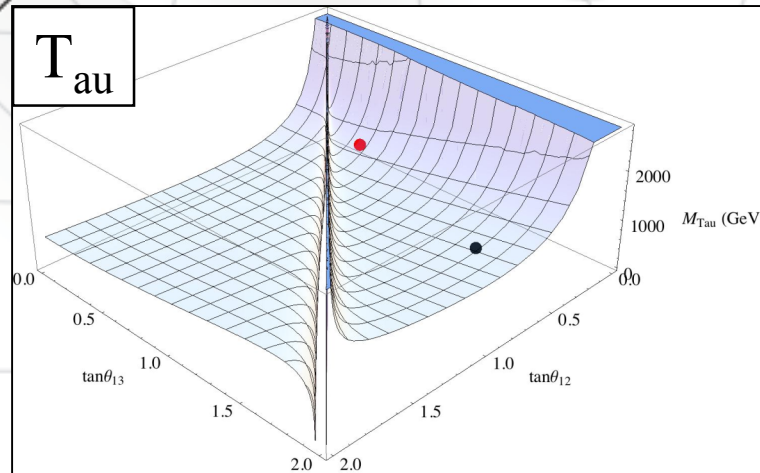
$$M_{W'}^2 = \frac{1}{4} (g_A^2 + g_B^2) (f^2 + F^2) - M_W^2$$

Particle Spectrum



- Note: Top partners are relatively light (required to avoid fine-tuning)

Heavy Top Masses - Dependence on Mixing Angles



$$\tan\theta_{12} \equiv y_1/y_2$$

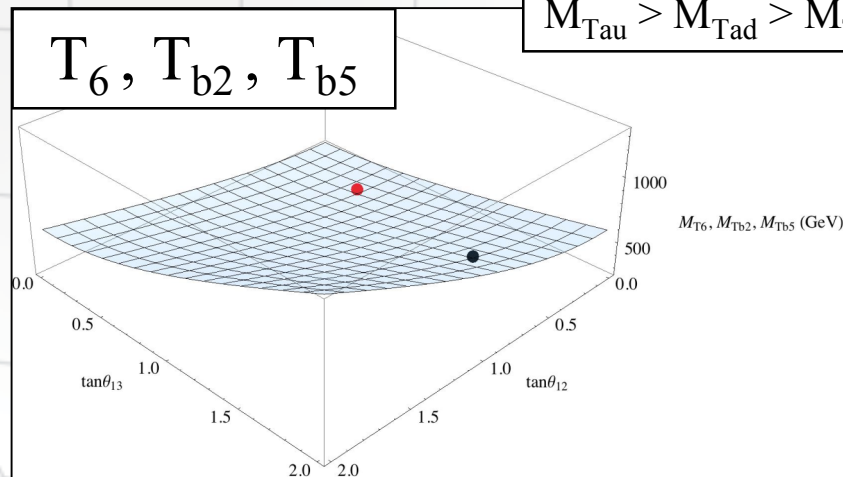
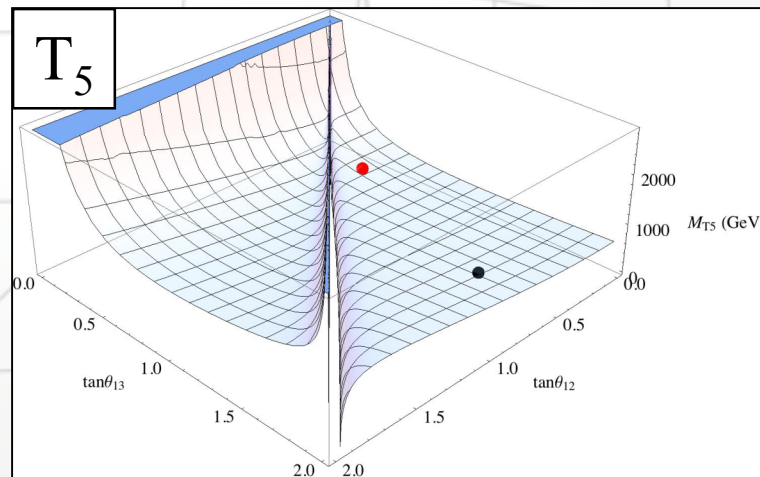
$$\tan\theta_{13} \equiv y_1/y_3$$

$$\tan\beta = \sqrt{3}$$

$$f = 1 \text{ TeV}$$

$$M_t = 172.0 \text{ GeV}$$

Choose $\tan\theta_{13} > \tan\theta_{12}$ so that
 $M_{T_{au}} > M_{T_{ad}} > M_{T_5} > M_{T_6}$



• $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

• $(\tan\theta_{12}, \tan\theta_{13}) = (0.325, 0.577)$

Heavy Top Branching Ratios



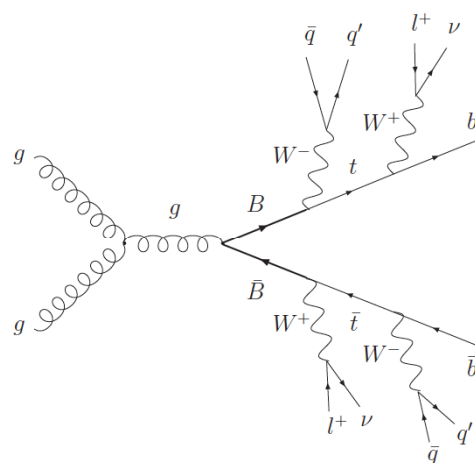
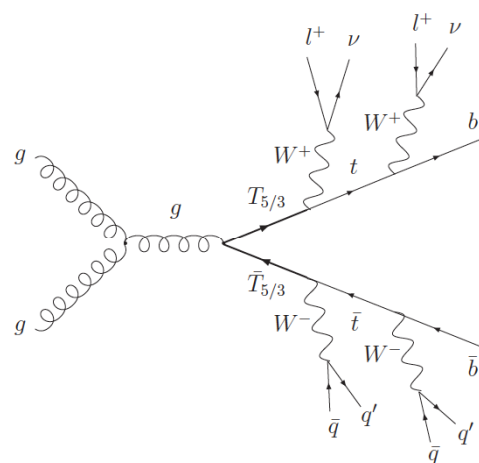
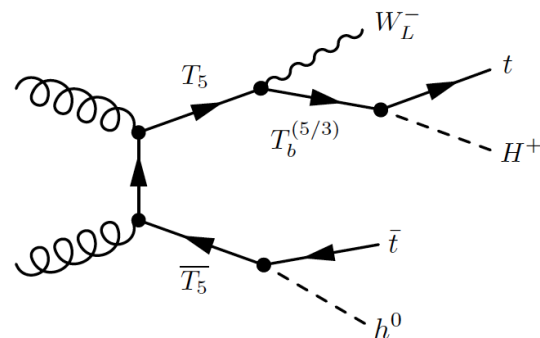
$(\tan\theta_{12}, \tan\theta_{13})$	• (0.727, 1.732)	• (0.325, 0.577)
Fermion Masses (GeV)		
M_{Tau}	1,142	1,065
M_{Tad}	1,131	1,056
M_{T5}	731	615
$M_{\text{T6}} = M_{\text{Tb2}} = M_{\text{Tb5}}$	665	326
Dominant T_5 Decay Modes ($M_h = 120$ GeV)		
	$\text{BR}(T_5 \rightarrow b W^+) = 0.480$	$\text{BR}(T_5 \rightarrow T_{b2} h) = 0.420$
	$\text{BR}(T_5 \rightarrow t Z) = 0.225$	$\text{BR}(T_5 \rightarrow T_{b5} W^-) = 0.269$
	$\text{BR}(T_5 \rightarrow t h) = 0.114$	$\text{BR}(T_5 \rightarrow T_{b2} Z) = 0.131$
		$\text{BR}(T_5 \rightarrow T_6 h) = 0.116$

- $\tan\beta = \sqrt{3}$, $M_t = 172.0$ GeV, $f = 1$ TeV
- Benchmark Point: $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$ for shorter decay chains

Heavy Top Pair Production



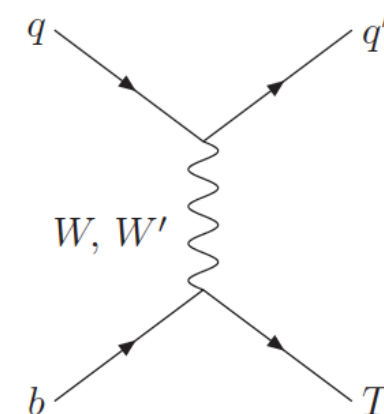
- Pair Production occurs via gluon fusion
- Cascade decays lead to many particles in the final state
- Pair Production of charge 5/3 and -1/3 heavy quarks leads to same sign dileptons (Contino, Servant, hep-ph/0801.1679v2)



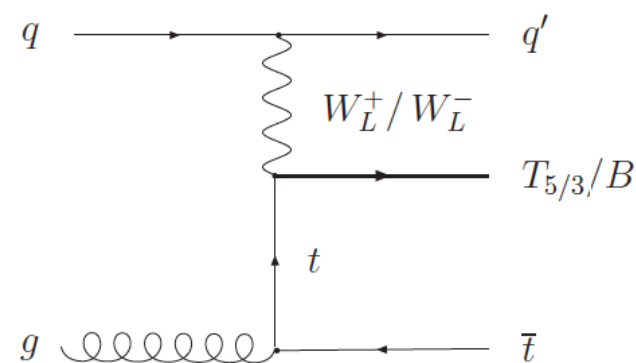
Heavy Top Single Production



- Single production of charge $2/3$ heavy quarks occurs via W exchange between light quark and b -quark partons



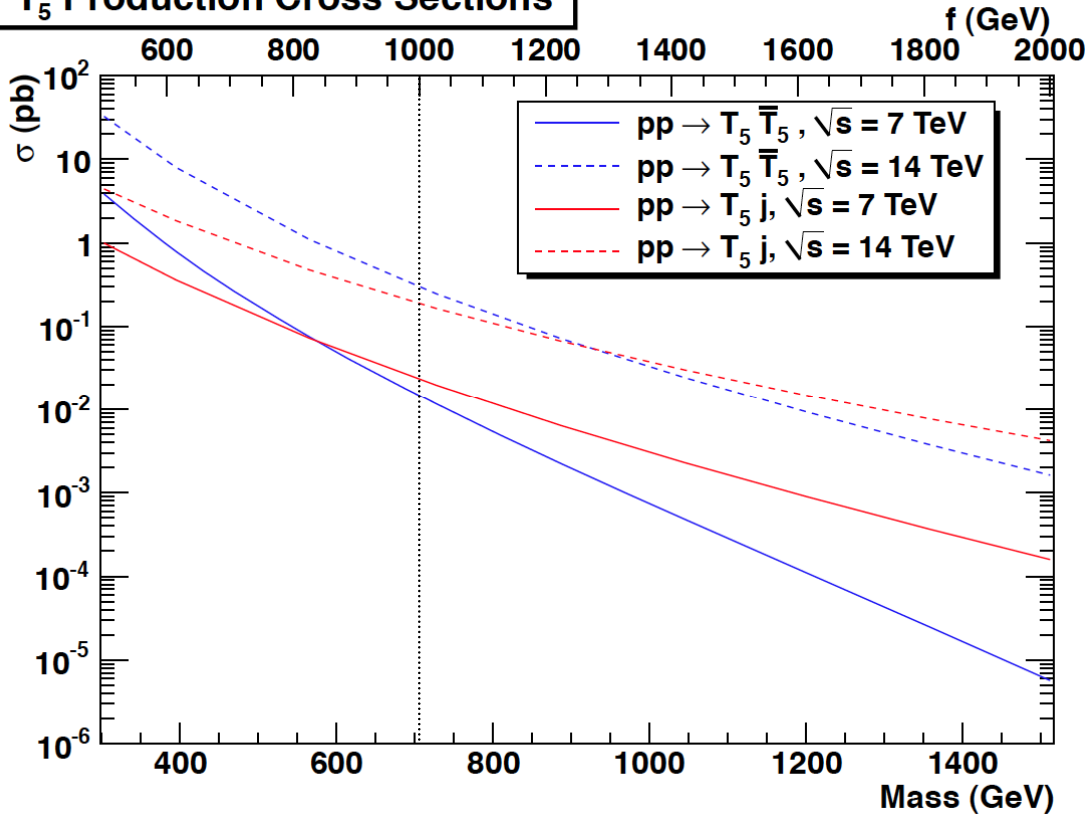
- Single production of charge $5/3$ and $-1/3$ quarks occurs in association with a top quark



T₅ Production



T₅ Production Cross Sections



Process ($f = 1 \text{ TeV}$)	$\sigma \text{ (fb), } 7 \text{ TeV}$	$\sigma \text{ (fb), } 14 \text{ TeV}$
Pair Production	11.555	244.98
Single Production	19.670	163.57

BRs for $f = 1 \text{ TeV}$,
 $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

Decay Mode	BR
$T_5 \rightarrow b W^+$	0.480
$T_5 \rightarrow t Z$	0.225
$T_5 \rightarrow t h$	0.114
$T_5 \rightarrow b H^+$	0.086
$T_5 \rightarrow t A^0$	0.068
$T_5 \rightarrow t H^0$	0.018
$T_5 \rightarrow \text{other}$	0.009

- σ calculated using MADGRAPH 5
- BRs calculated using BRIDGE

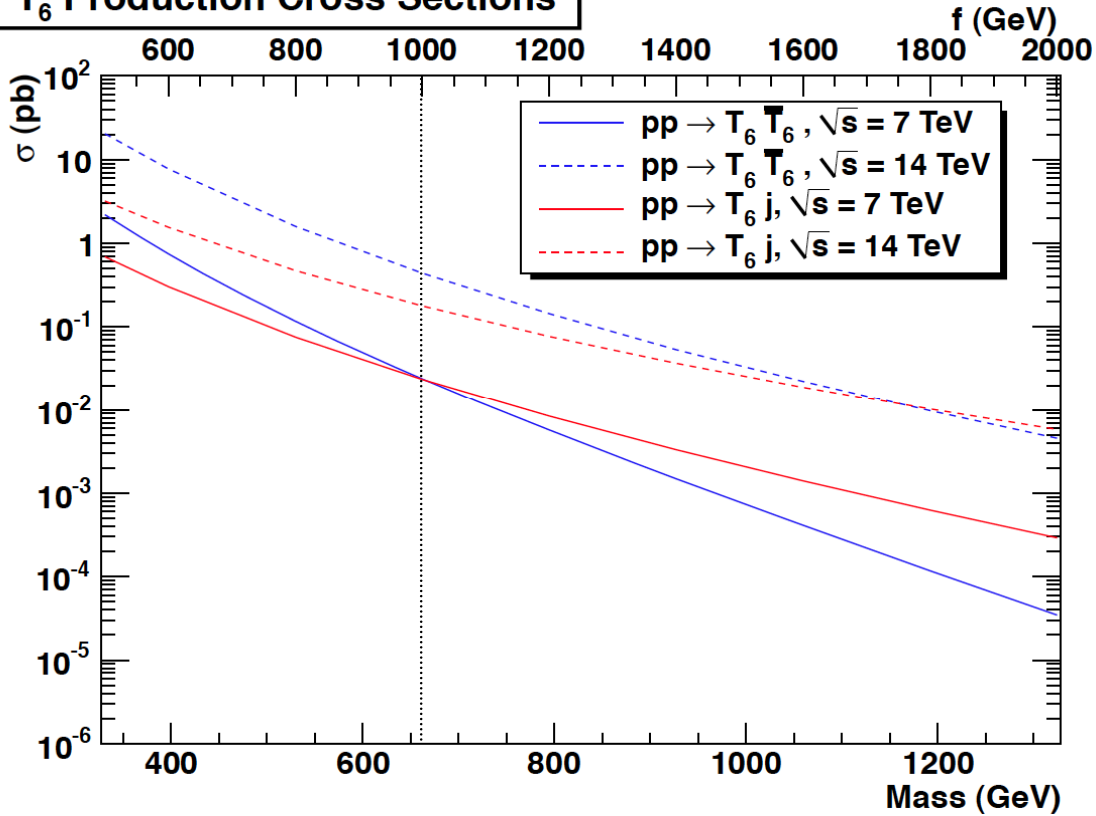
$$M_h = 120 \text{ GeV}, \quad M_{H^0} = 505 \text{ GeV}$$

$$M_{H^\pm} = M_{A^0} = 500 \text{ GeV}$$

T₆ Production



T₆ Production Cross Sections

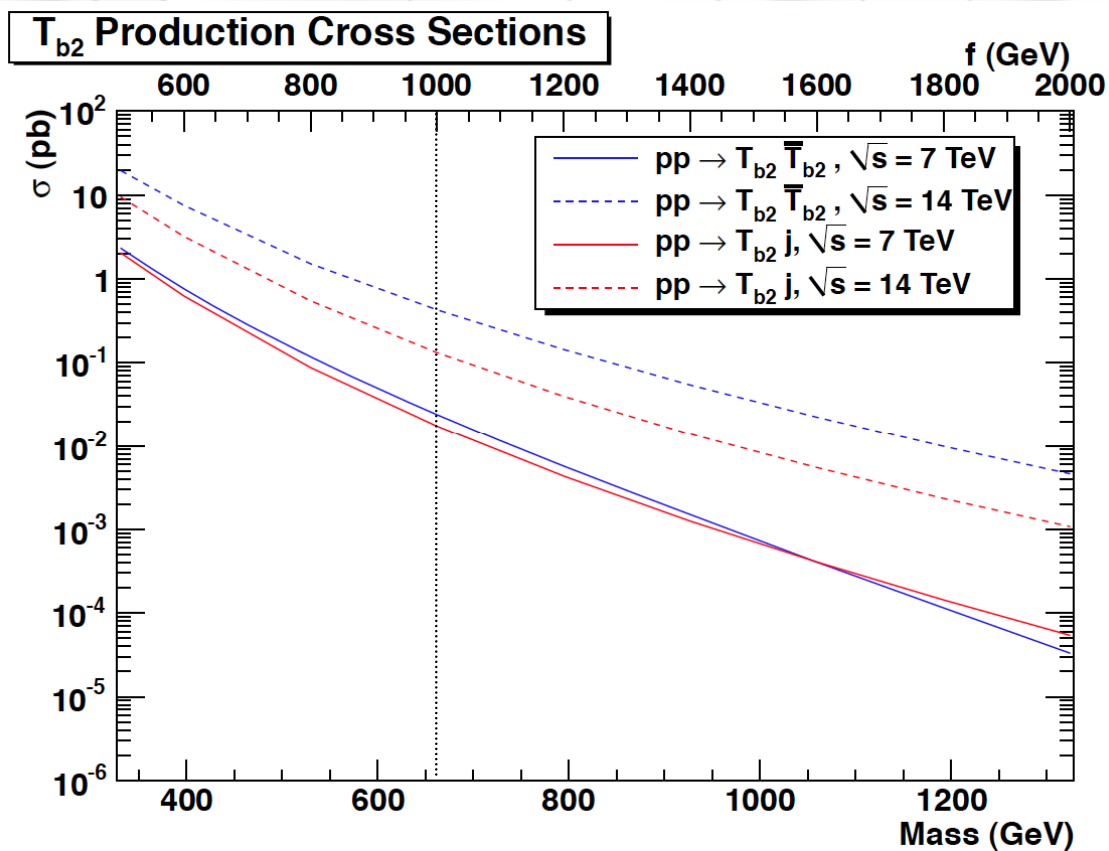


BRs for $f = 1 \text{ TeV}$,
 $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

Decay Mode	BR
$T_6 \rightarrow b W^+$	0.416
$T_6 \rightarrow t h$	0.207
$T_6 \rightarrow b H^+$	0.192
$T_6 \rightarrow t Z$	0.170
$T_6 \rightarrow \text{other}$	0.015

Process ($f = 1 \text{ TeV}$)	$\sigma \text{ (fb), } 7 \text{ TeV}$	$\sigma \text{ (fb), } 14 \text{ TeV}$
Pair Production	23.862	439.82
Single Production	23.481	178.09

T_{b2} Production



BRs for $f = 1 \text{ TeV}$,
 $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

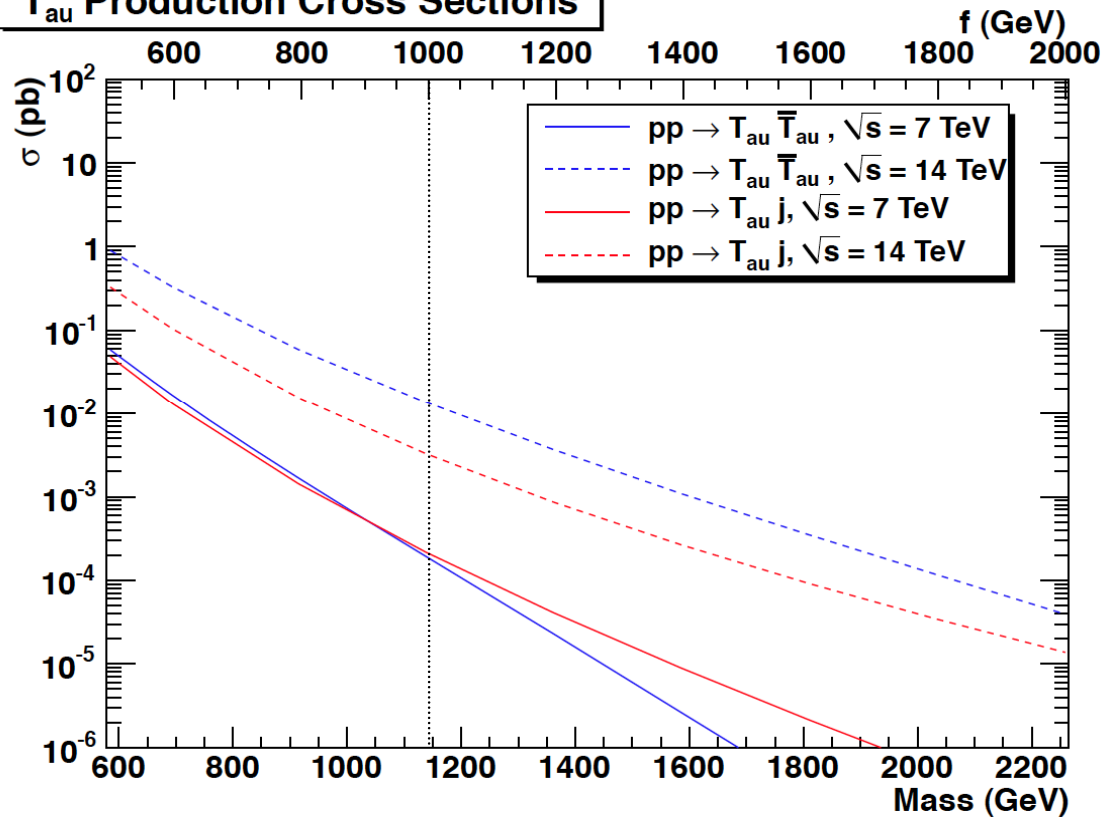
Decay Mode	BR
$T_{b2} \rightarrow t Z$	0.491
$T_{b2} \rightarrow b W^+$	0.258
$T_{b2} \rightarrow t h$	0.217
$T_{b2} \rightarrow b H^+$	0.012
$T_{b2} \rightarrow \text{other}$	0.022

Process ($f = 1 \text{ TeV}$)	σ (fb), 7 TeV	σ (fb), 14 TeV
Pair Production	23.982	427.67
Single Production	17.457	131.98

T_{au} Production



T_{au} Production Cross Sections



Process ($f = 1 \text{ TeV}$)	$\sigma \text{ (fb), } 7 \text{ TeV}$	$\sigma \text{ (fb), } 14 \text{ TeV}$
Pair Production	0.19434	13.736
Single Production	0.21811	3.2883

BRs for $f = 1 \text{ TeV}$,
 $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

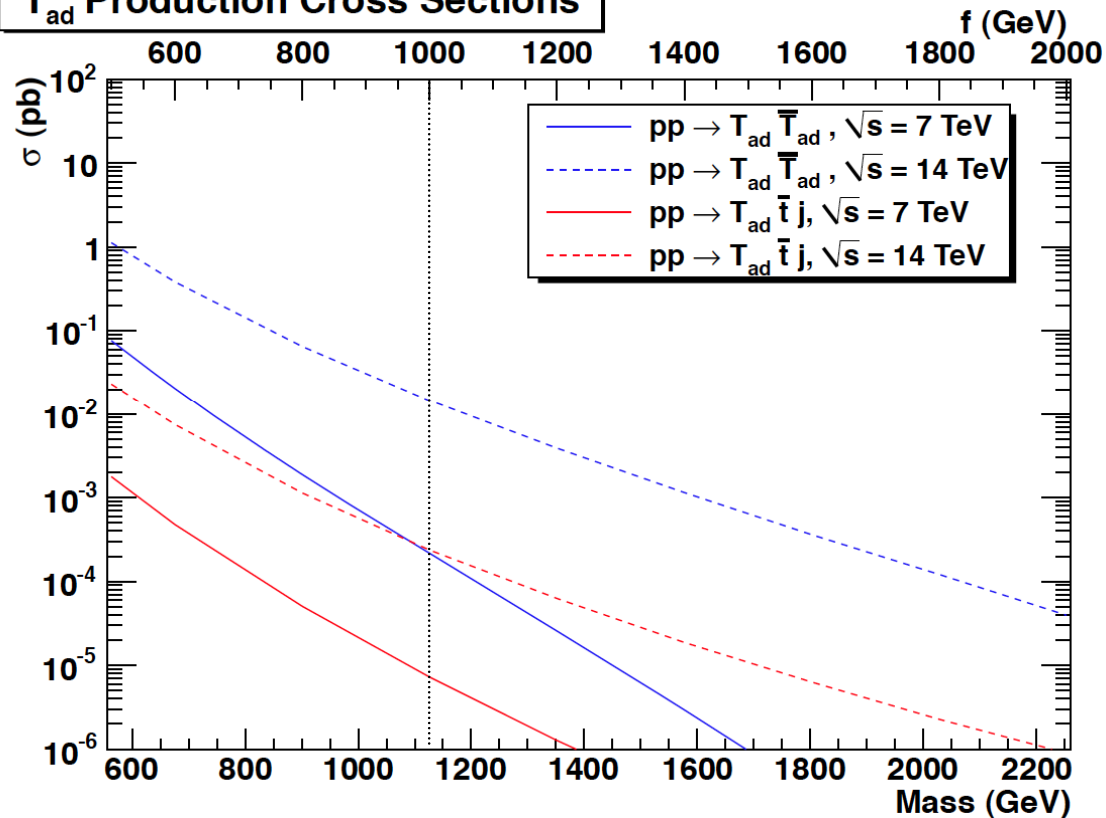
Decay Mode	BR
$T_{au} \rightarrow T_5 Z$	0.334
$T_{au} \rightarrow T_{b2} Z$	0.118
$T_{au} \rightarrow T_{b2} h$	0.115
$T_{au} \rightarrow T_6 Z$	0.086
$T_{au} \rightarrow T_5 h$	0.084
$T_{au} \rightarrow T_6 h$	0.083
$T_{au} \rightarrow t Z$	0.082
$T_{au} \rightarrow b W^+$	0.058
$T_{au} \rightarrow T_{b5} W^-$	0.015
$T_{au} \rightarrow \text{other}$	0.025

Could adjust parameters so that T_{au} is lighter and more easily produced

T_{ad} Production (charge -1/3)



T_{ad} Production Cross Sections



Process ($f = 1 \text{ TeV}$)	σ (fb), 7 TeV	σ (fb), 14 TeV
Pair Production	0.21616	14.515
Single Production	0.0072314	0.23632

BRs for $f = 1 \text{ TeV}$,
 $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

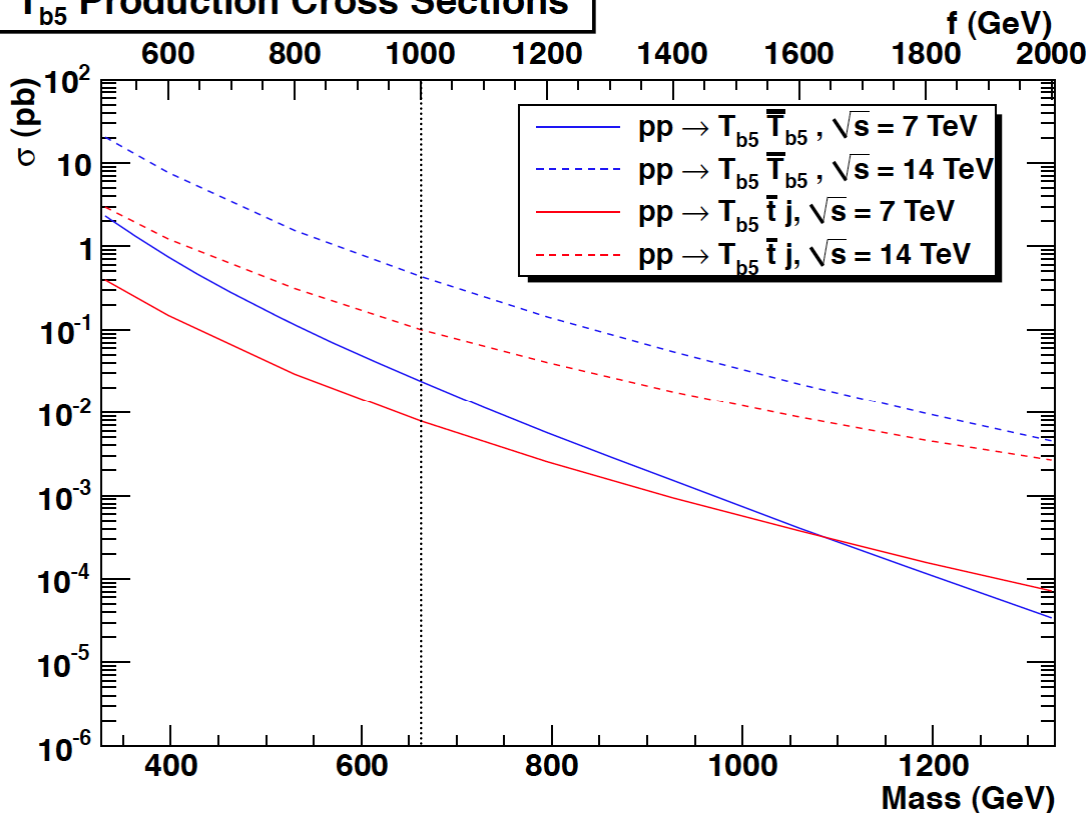
Decay Mode	BR
$T_{ad} \rightarrow T_5 W^-$	0.631
$T_{ad} \rightarrow T_6 W^-$	0.164
$T_{ad} \rightarrow T_{b2} W^-$	0.138
$T_{ad} \rightarrow t W^-$	0.028
$T_{ad} \rightarrow \text{other}$	0.039

Could adjust parameters so that T_{ad} is lighter and more easily produced

T_{b5} Production (charge 5/3)



T_{b5} Production Cross Sections



BRs for $f = 1 \text{ TeV}$,
 $(\tan\theta_{12}, \tan\theta_{13}) = (0.727, 1.732)$

Decay Mode	BR
$T_{b5} \rightarrow t W^+$	0.982
$T_{b5} \rightarrow \text{other}$	0.018

Process ($f = 1 \text{ TeV}$)	$\sigma \text{ (fb)}, 7 \text{ TeV}$	$\sigma \text{ (fb)}, 14 \text{ TeV}$
Pair Production	23.977	435.41
Single Production	7.8771	100.24

Conclusions & Future Work



- The Bestest Little Higgs Model generates a custodially symmetric Higgs quartic and avoids fine-tuning in the top sector
- Several top partners that are lighter than heavy gauge bosons, leading to interesting phenomenology in heavy fermion sector
- Production cross sections and branching ratios of heavy top quarks were calculated for a specific parameter set for a 7 TeV and 14 TeV LHC
- Must explore parameter space more fully and determine its effect on production cross sections and branching ratios
- Must simulate heavy top quark decays and consider backgrounds to final states

Backup Slides



The Littlest Higgs Model

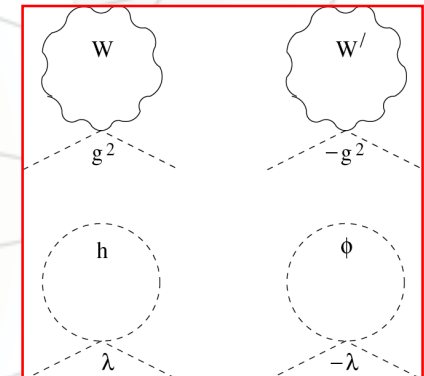
N. Arkani-Hamed et al. (2002) hep-ph/0206021



- Introduce new interactions at scale $\Lambda = 4\pi f \sim 10$ TeV with new particles at $f \sim 1$ TeV: heavy gauge bosons, heavy scalars, new heavy quarks.

- Quadratic divergences in M_H^2 are cancelled by the contributions of these new particles.

$$\delta M_H^2 = \frac{G_F \Lambda^2}{4\sqrt{2}\pi^2} (6M_W^2 + 3M_Z^2 + M_H^2 - 12M_t^2) + \dots$$



- Scalar Sector:

$$h = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix}$$

Doublet

$$\phi = \begin{pmatrix} \phi^{++} & \phi^+/\sqrt{2} \\ \phi^+/\sqrt{2} & \phi^0 \end{pmatrix}$$

Triplet

Littlest Higgs with Custodial SU(2)

Chang (2004) hep-ph/0306034v3



- Little Higgs Model with Left-Right Symmetry
- $SO(9) \rightarrow SO(5) \times SO(4) \supset SU(2)_L \times SU(2)_R \times SU(2)_W \times U(1)_Y$
- Scalar Sector:
 - Complex Higgs Doublet: h
 - 3 Real Triplets: ϕ^{ab} ($a, b = 1, 2, 3$)
 - Real Singlet: ϕ^0

$$\langle \Sigma \rangle = \begin{pmatrix} 0 & 0 & \mathbb{1}_4 \\ 0 & 1 & 0 \\ \mathbb{1}_4 & 0 & 0 \end{pmatrix}$$

$$\Sigma = e^{i\Pi/f} \langle \Sigma \rangle e^{i\Pi^T/f} = e^{2i\Pi/f} \langle \Sigma \rangle$$

$$\Pi = \frac{-i}{4} \begin{pmatrix} 0 & \sqrt{2}\vec{h} & -\Phi \\ -\sqrt{2}\vec{h}^T & 0 & \sqrt{2}\vec{h}^T \\ \Phi & -\sqrt{2}\vec{h} & 0 \end{pmatrix}$$

Littlest Higgs with Custodial SU(2)

Chang (2004) hep-ph/0306034v3



- Begin by constructing a Lagrangian:

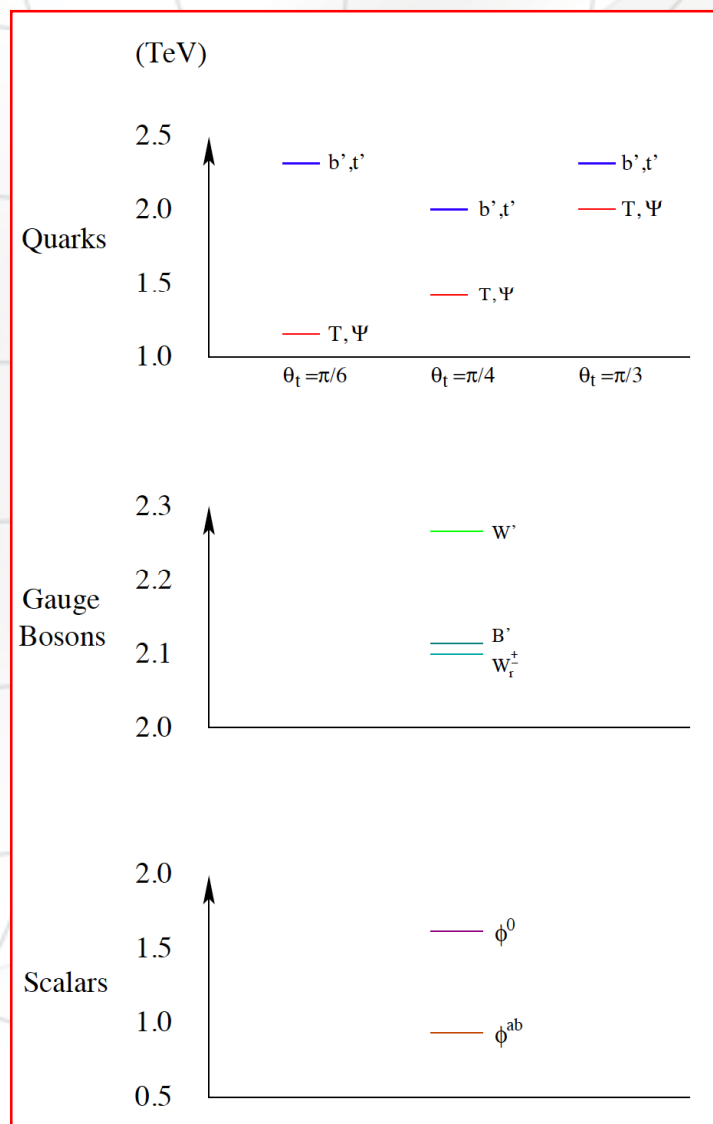
- Top Sector:

$$\mathcal{L}_{top} = y_1 f (\vec{\chi}^c T t^c 0_4) \Sigma \begin{pmatrix} 0_5 \\ \vec{q}_t \end{pmatrix} + y_2 f \vec{\chi}^T \vec{\chi}^c + \text{h.c.}$$

- Gauge Sector:

$$\mathcal{L}_{kin} = \frac{f^2}{4} \text{Tr} [D_\mu \Sigma D^\mu \Sigma]$$

$$D_\mu \Sigma = \partial_\mu \Sigma + i [A_\mu, \Sigma]$$



Littlest Higgs with Custodial SU(2)

Chang (2004) [hep-ph/0306034v3](#)



- Radiative corrections generate a Coleman-Weinberg Potential:

$$V = \lambda_1^- f^2 (\phi^0 - H^0)^2 + \lambda_1^+ f^2 (\phi^0 + H^0)^2 \\ + \lambda_3^- f^2 (\phi^{ab} - H^{ab})^2 + \lambda_3^+ f^2 (\phi^{ab} + H^{ab})^2 + \Delta\lambda_3 f^2 (\phi^{a3} + H^{a3})^2 + \mu^2 h^\dagger h$$

where $\Delta\lambda_3 \ll \lambda_3^\pm$

- EWSB occurs when neutral scalars acquire vevs that minimize the potential
- Shift scalar fields by their vevs and determine the interactions of the theory
 $h \rightarrow h + v \quad \phi^0 \rightarrow \phi^0 + v_0 \quad \phi^{aa} \rightarrow \phi^{aa} + v_a \quad (v_1 = v_2 \approx v_3)$
- One can then determine mass eigenstates and calculate Feynman rules

Dangerous Singlet Problem

Schmaltz, Thaler (2009) [hep-ph/0812.2477v3](#)



- Collective Quartic:

$$V \sim \lambda_1^- f^2 (\phi^0 - H^0)^2 + \lambda_1^- f^2 (\phi^0 + H^0)^2 \quad \text{where } H^0 = h^\dagger h / (4f)$$

- Radiative corrections generate operators of the form:

$$- \lambda_1^- f^3 (\phi^0 - H^0 + \dots) + \lambda_1^+ f^3 (\phi^0 + H^0 + \dots)$$

which preserve the shift symmetries:

$$h \rightarrow h + \varepsilon + \dots \quad \text{and} \quad \phi^0 \rightarrow \phi^0 \pm (h^\dagger \varepsilon + \varepsilon^\dagger h) / (4f) + \dots$$

- In order to prevent quadratically divergent Higgs mass terms and ϕ^0 tadpoles at the one-loop level, additional symmetries on ϕ^0 are required.
- There is no viable one-Higgs doublet Little Higgs model where a collective quartic involves a real singlet

Fermion Sector



- To build Yukawa interactions, Fermions must transform under $SO(6)_A$ or $SO(6)_B$

$$SO(6)_A: \quad Q^T = \left(\frac{1}{\sqrt{2}}(-Q_{a1} - Q_{b2}) \quad \frac{i}{\sqrt{2}}(Q_{a1} - Q_{b2}) \quad \frac{1}{\sqrt{2}}(Q_{a2} - Q_{b1}) \quad \frac{i}{\sqrt{2}}(Q_{a2} + Q_{b1}) \quad Q_5 \quad Q_6 \right)$$

$$SO(6)_B: \quad (U^c)^T = \left(\frac{1}{\sqrt{2}}(-U_{b1}^c - U_{a2}^c) \quad \frac{i}{\sqrt{2}}(U_{b1}^c - U_{a2}^c) \quad \frac{1}{\sqrt{2}}(U_{b2}^c - U_{a1}^c) \quad \frac{i}{\sqrt{2}}(U_{b2}^c + U_{a1}^c) \quad U_5^c \quad U_6^c \right)$$

$$SU(2)_A \text{ doublet: } Q_a'^T \rightarrow \frac{1}{\sqrt{2}}(-Q'_{a1}, iQ'_{a1}, Q'_{a2}, iQ'_{a2}, 0, 0)$$

$$SU(2)_B \text{ singlet: } U_5'^{cT} \rightarrow (0, 0, 0, 0, U_5'^c, 0) \quad S = \text{diag}(1, 1, 1, 1, -1, -1)$$

Identifying Q_a with SM quark doublet ($Y=1/6$) requires additional $U(1)$ symmetry

$$T_Y = T_R^3 + T_X$$

	$SO(6)_A$	$SO(6)_B$	$SU(3)_C$	$U(1)_X$
Q	6	—	3	$2/3$
Q'_a	2^(*)	—	3	$2/3$
U^c	—	6	$\bar{\mathbf{3}}$	$-2/3$
$U_5'^c$	—	1^(*)	$\bar{\mathbf{3}}$	$-2/3$